

Two-Way Relaying with Multiple Antennas using Covariance Feedback

Winston Ho and
Ying-Chang Liang,
Institute for Infocomm Research
(I²R), Singapore

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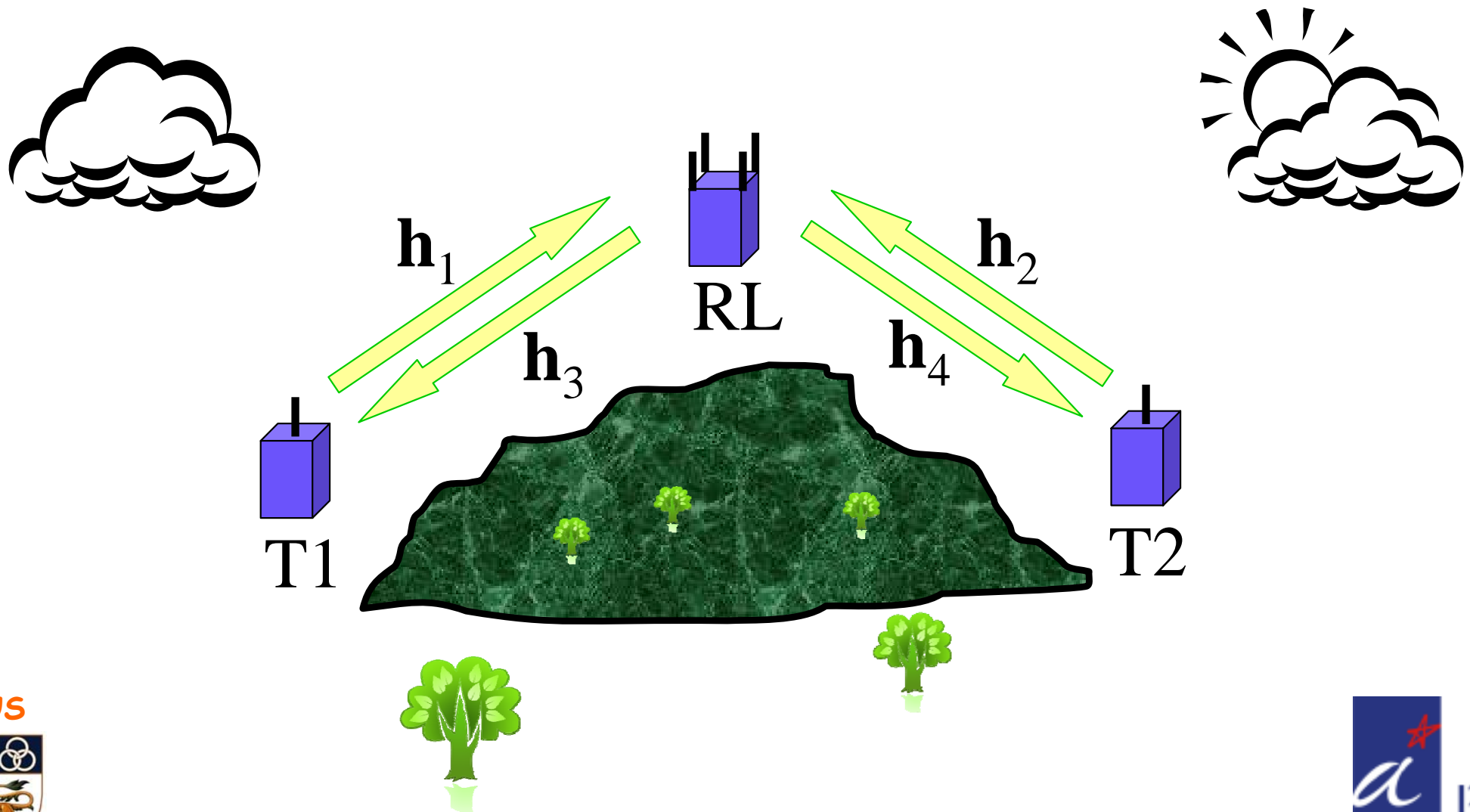


VTC 2008 Fall, Calgary



Introduction

Physical-layer Network Coding (PNC)



Sum Rate Maximization given Instantaneous CSI

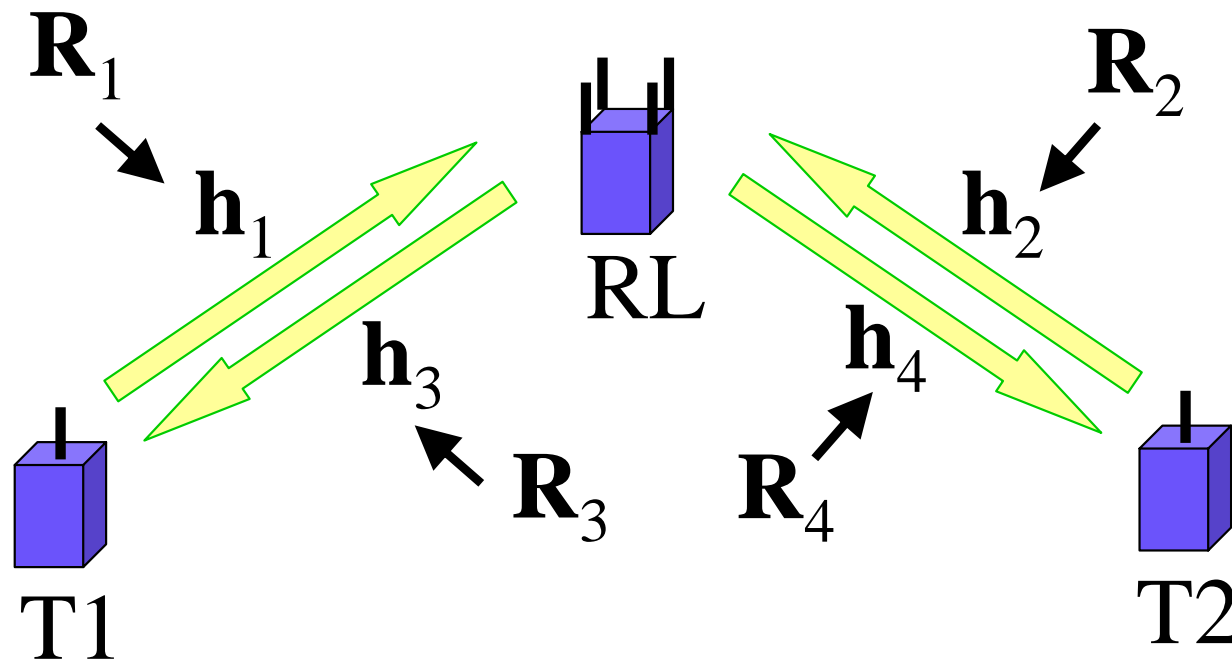
$$\underset{\mathbf{A}}{\text{maximize}} \quad r(\mathbf{A}) = 0.5(r_1(\mathbf{A}) + r_2(\mathbf{A}))$$

$$\text{subject to} \quad \gamma_3 \leq \bar{\gamma}_3$$

- [5] Y.-C. Liang and R. Zhang, "Optimal Analogue Relaying with Multi-Antennas for Physical Layer Network Coding," *Proc. Int. Conf. Commun.*, pp. 3893-3897, May. 2008.



Sum Rate Maximization given Covariance CSI (1)



Sum Rate Maximization given Covariance CSI (2)

$$\begin{aligned} & \underset{\mathbf{A}}{\text{maximize}} && E[r(\mathbf{A})] = E[0.5(r_1(\mathbf{A}) + r_2(\mathbf{A}))] \\ & \text{subject to} && E[\gamma_3] \leq \bar{p}_3 \end{aligned}$$

Sum Rate Maximization given Covariance CSI (3)

✚ Sample Average Approximation (SAA)

- ✚ Overestimate (“SAA1”)

- ✚ Underestimate (“SAA2”)

- ✚ Optimality gap

- ✚ [15] A. J. Kleywegt, A. Shapiro, and T. Homem-de-Mello, “The sample average approximation method for stochastic discrete optimization,” *SIAM Journal on Optimization*, vol. 12, no. 2, pp. 479--502, 2002.

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Low-complexity Solutions based on Covariance CSI (1)

✚ Method 1:

✚ Instantaneous Equivalent Rate Maximization (IER-Max)

✚ Principle eigenvectors

$$\underset{\mathbf{G}}{\text{maximize}} \quad \tilde{r}(\mathbf{G}) = 0.5(\tilde{r}_1(\mathbf{G}) + \tilde{r}_2(\mathbf{G}))$$

$$\text{subject to} \quad \tilde{\gamma}_3 \leq \bar{p}_3$$



Low-complexity Solutions based on Covariance CSI (2)

Method 2:

MRR-MRT

Principle eigenvectors: $\mathbf{F}_A = [\mathbf{u}_1, \mathbf{u}_2] \in \mathbb{C}^{M \times 2}$
 $\mathbf{F}_B = [\mathbf{u}_4^T; \mathbf{u}_3^T] \in \mathbb{C}^{2 \times M}$

$$\mathbf{A} = \alpha \mathbf{F}_B^H \mathbf{F}_A^H$$

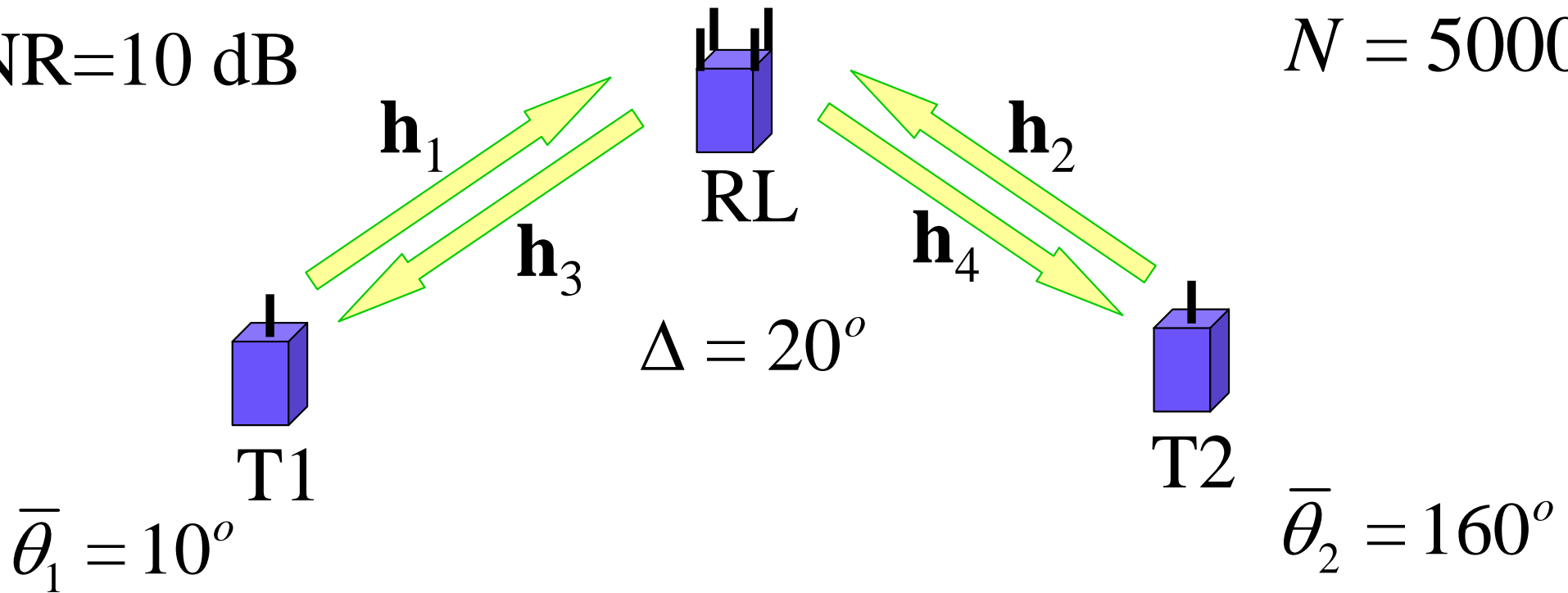
Simulations

$$f_A = f_1 = f_2 = 1.8 \text{ GHz}$$

$M = 4$ antennas

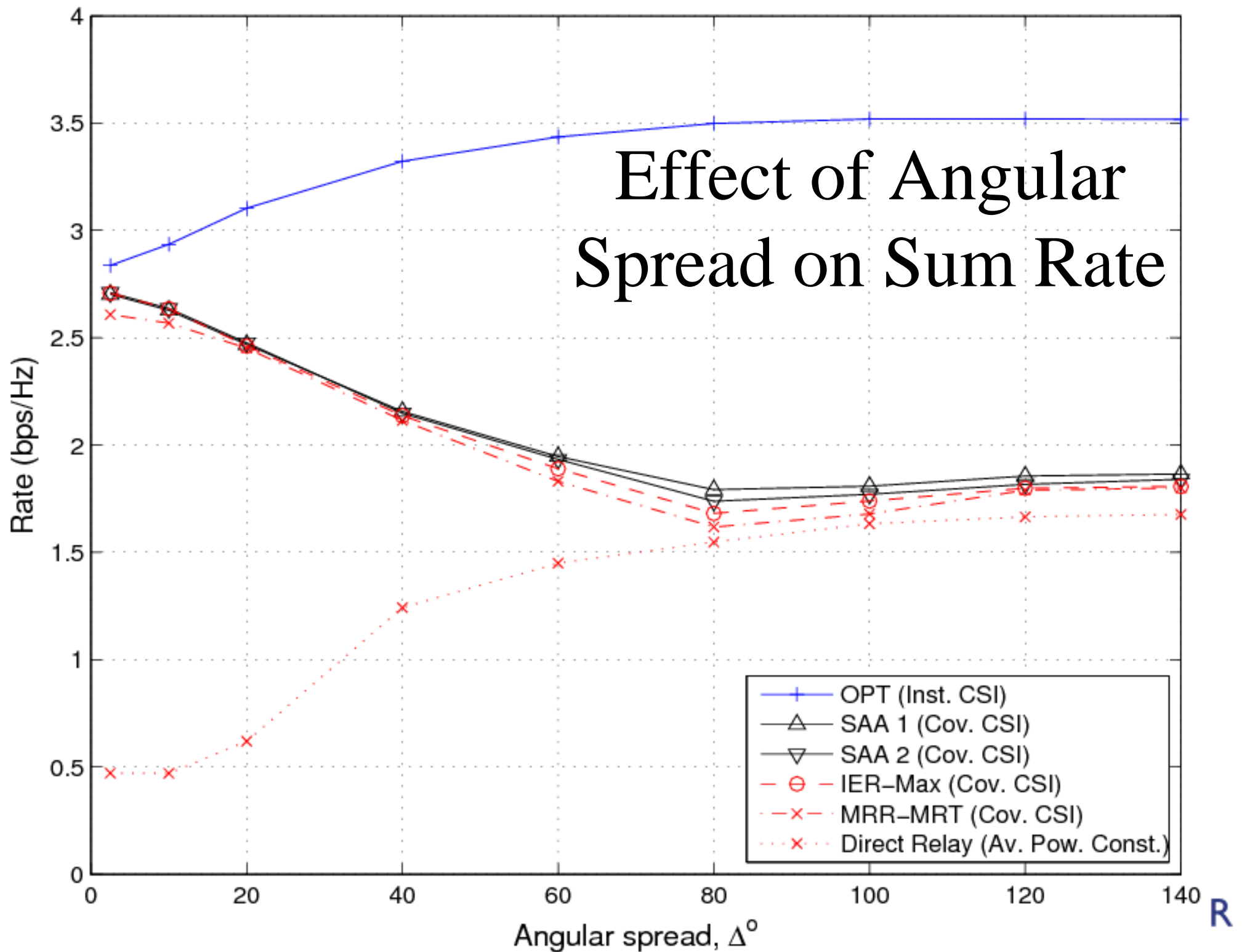
SNR=10 dB

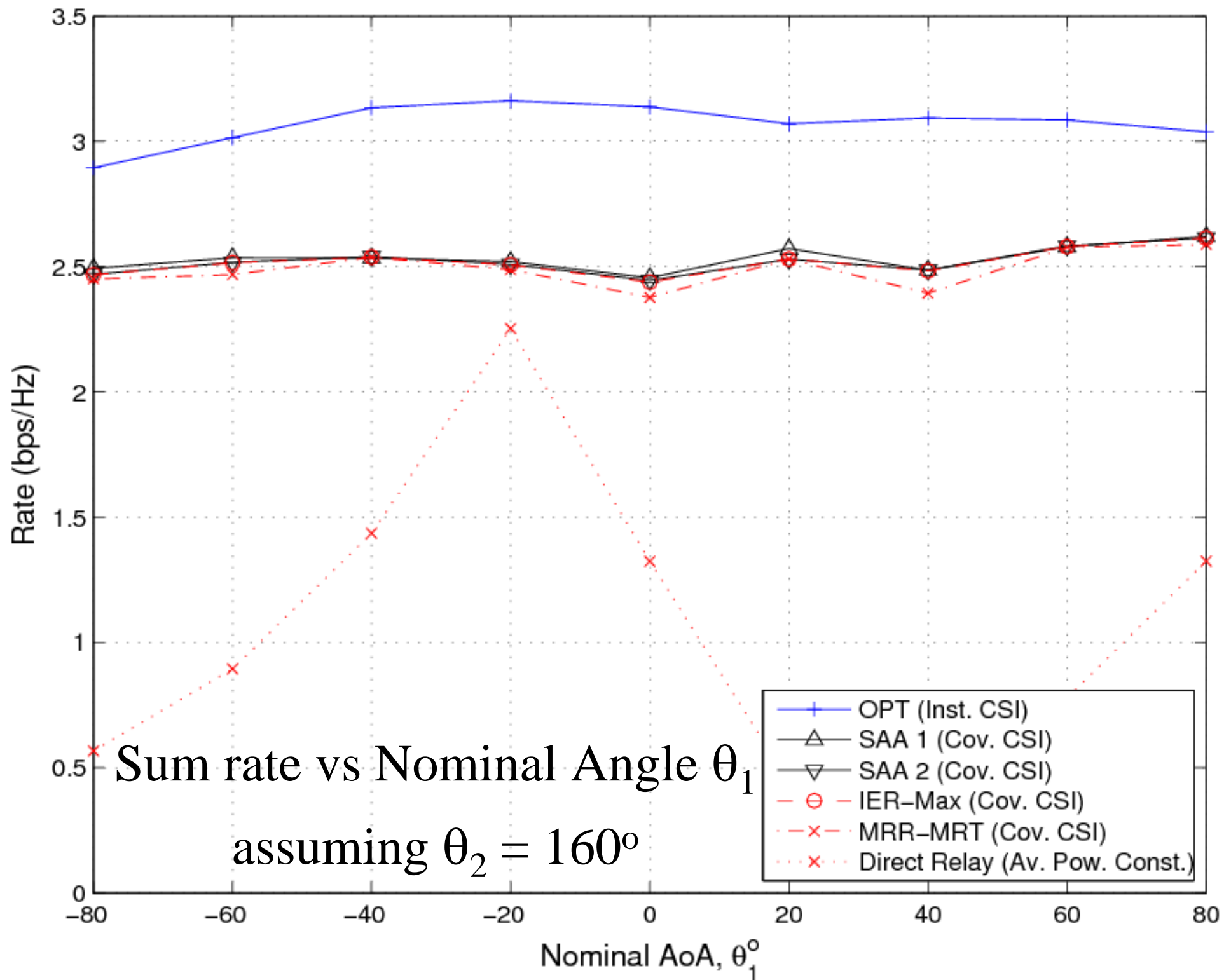
$N = 5000$



$$f_B = f_3 = f_4 = 2.6 \text{ GHz}$$

Effect of Angular Spread on Sum Rate





Conclusion

- ✚ Two-way relaying
- ✚ Physical layer network coding
- ✚ Multiple antennas
- ✚ Sum rate maximization
- ✚ Covariance feedback
- ✚ Efficient near-optimal methods
- ✚ Angular spread, nominal angles